CS310 Computational Geometry Spring 2019

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Assignment 2

1. Let P be a polygon with n vertices $v_0, ..., v_{n-1}, v_i = (x_i, y_i)$ ordered counterclockwise in the plane. Prove that the area of P is:

$$\frac{1}{2} \sum_{i=0}^{n-1} (x_i y_{i+1} - x_{i+1} y_i)$$

- 2. Exercise 1.21. Obviously, you should not list figures for all, but describe how your figure/construction generalizes.
- **3.** Exercise 1.22.
- **4.** Prove or disprove: every polygon with an even number of vertices may be partitioned by diagonals into convex quadrilaterals. What about just quadrilaterals, not necessarily convex?
- 5. The dual graph of any triangulation of a simple polygon is a free tree (we discussed this in class). A free tree is a *path* if it has no vertices of degree greater than two. Keep in mind that a polygon may have many different triangulations (see Figure 1). Prove or disprove: Every monotone polygon has a triangulation whose dual graph is a path. (If you prove this statement, you will need to show that you can always find a triangulation whose dual is a path. If you disprove it, you will need to show an example of a monotone polygon that has no triangulation whose dual is a path.)

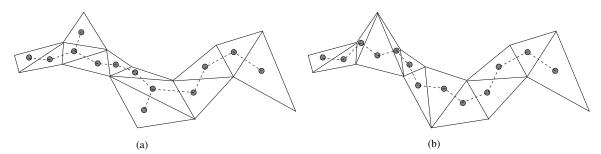


Figure 1: Two triangulations of the same polygon. (a) Dual is not a path. (b) Dual is a path.

- **6.** Given n points in the plane, sorted by x-coordinates, describe an algorithm which constructs a simple polygon whose vertices are those points. There may be many such polygons; your algorithm needs to output just one. Your algorithm should run in O(n) time. Show that it does.
- 7. There is a two-piece dissection of the 18x18 square to the left, and the 23x15 rectangle to the right with a centrally placed 7x3 hole, see Figure 2. Each is composed of 324 unit squares. Try to find the dissection!
- 8. Show that a regular tetrahedron can not be scissors congruent with a cube.

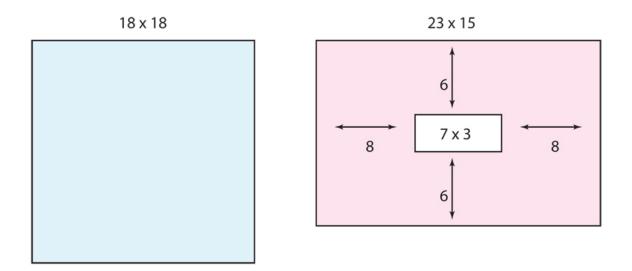


Figure 2: There is a two-piece dissection that takes one figure to the other