

These questions relate to lecture material and aim to highlight the most important concepts. We will cover questions similar to these for our midterm.

1. Verify that multiplying the quaternion  $i = [0, (1,0,0)]$  by  $j = [0, (0,1,0)]$  produces the quaternion  $k = [0, (0,0,1)]$

2. Show that the quaternions  $q$  and  $-q$  represent the same rotation.

3. Consider the geometric derivation of the control point  $b_2$ .

Check that  $p_{i+1} - \text{Bisect}(p_i, \text{Double}(p_{i+2}, p_{i+1})) = 0.5 * (p_{i+2} - p_i)$

4. Consider the vectors  $A = (1,1,0)$  and  $B = (1,0,0)$ . Decompose  $A$  into two vectors, one which is parallel to  $B$  and one that is perpendicular to  $B$ .

5. Consider the same vectors  $A$  and  $B$  from the previous question. Reflect the vector  $A$  around  $B$ .